Monte-Carlo Tracer Particles

RUM 2017, Nice

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Outline

Introduction

Different methods

- Velocity method
- Monte Carlo method

MC Implementation

Is it working?

Discussion

Introduction

Eulerian & Lagrangian

Eulerian code (AMR like):

- no subgrid information
- no Lagrangian history of gas

Is it possible to overcome this issue?

From passive scalar to tracers

- Where does the gas come from?

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- ... [TBC]

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- Passive
- *Behave* like the gas on average
- Like individual H/He nuclei

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Computational properties

- Cheap (CPU? RAM?)
- Go where the gas goes (star, sinks, grid, dust, ...)

Different methods

Velocity method

Move tracers using tri-linear interpolation of the velocity

$$v_i^p = \text{interpolation} \sum_{\text{neighbor } j} v_j \tag{1}$$

Pros

- smooth Lagrangian history (trace velocity)
- already implemented in RAMSES!

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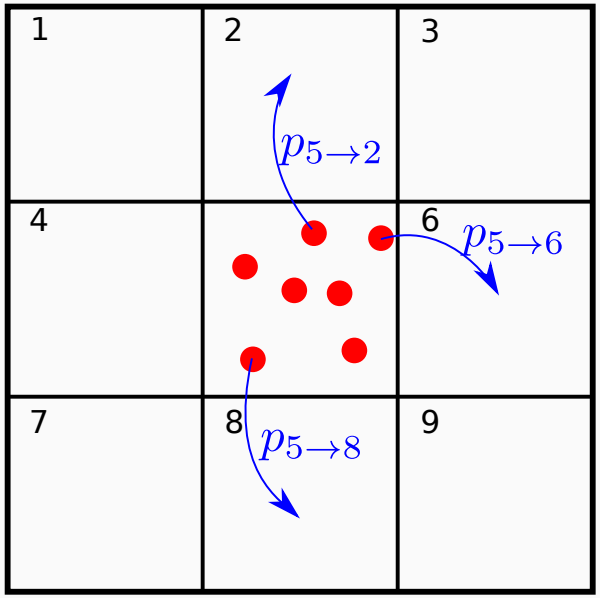
Cons

- *does not* follow the gas density: $\int \mathrm{d}S v_i^p \rho \neq \text{flux}$
- how to trace stars? AGN?
- quite CPU expensive

Monte Carlo method

Move tracers following flux

$$p_{i\to j} = \frac{\text{mass flux}_{i\to j}}{M_i}$$



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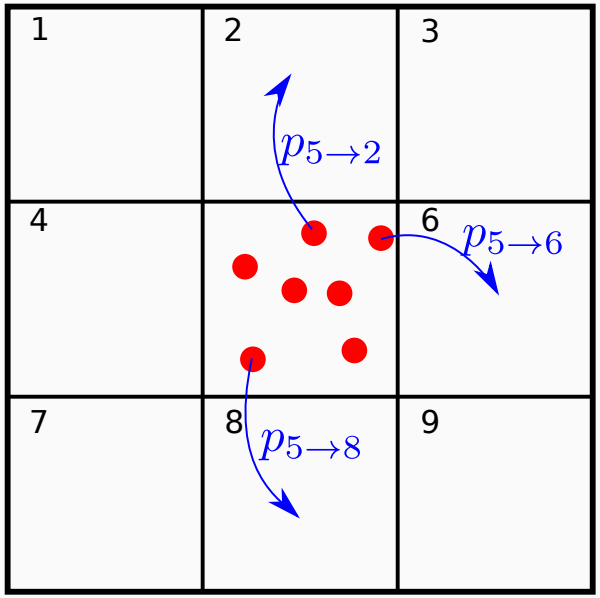

Pros

- CPU cheap
- follow gas density
- precision $\propto N_{\text{tracers}}$
- move onto stars, sinks, ...

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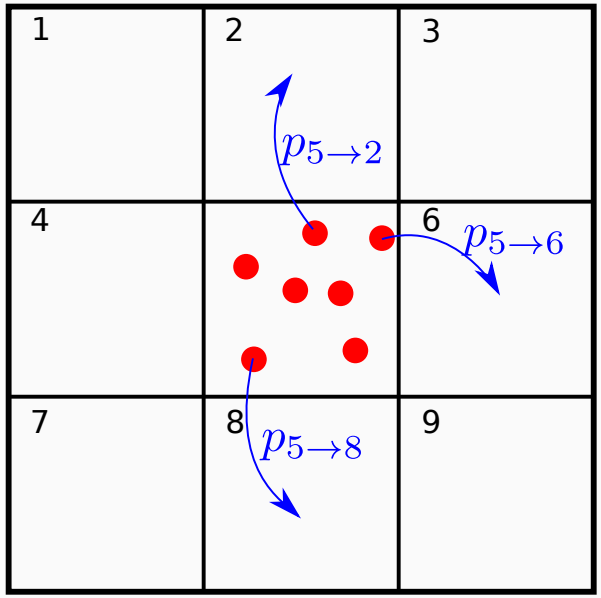

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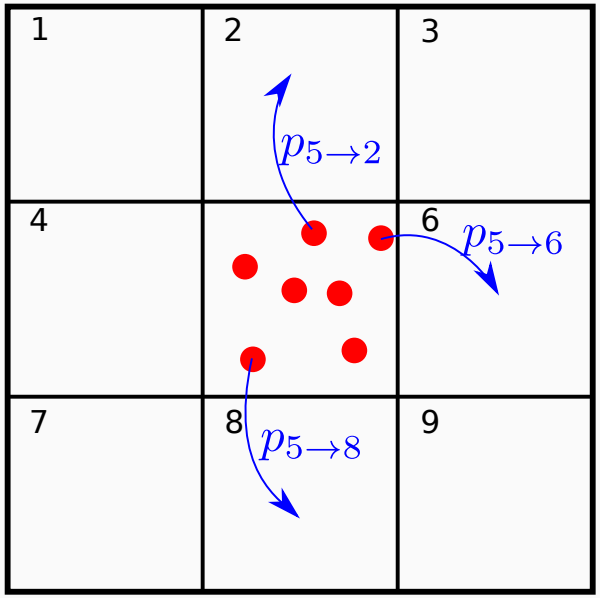

Pros

- CPU cheap
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- move onto stars, sinks, ...
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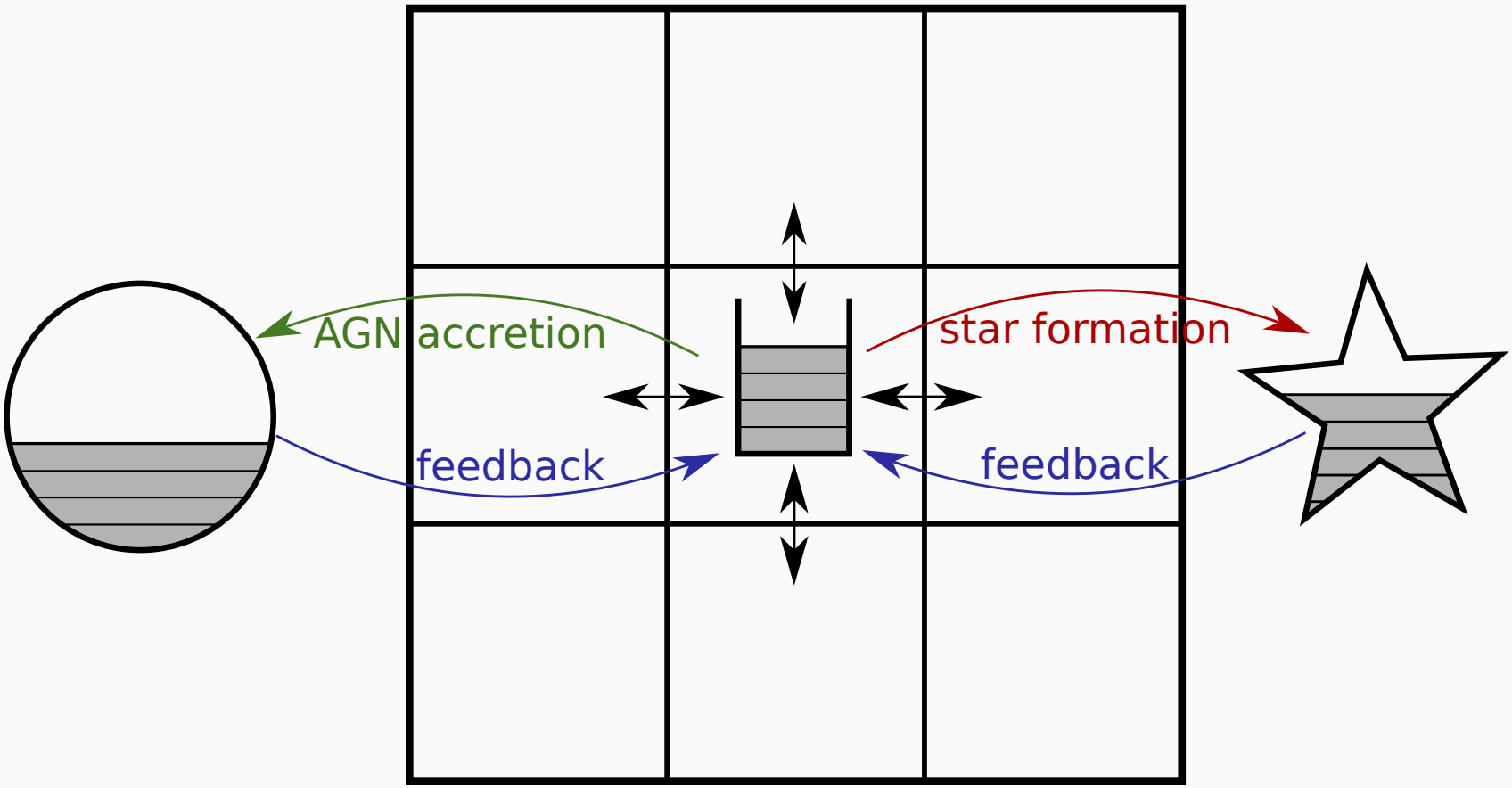
Cons

- RAM expensive
- noisy Lagrangian history

MC Implementation

Scheme



Equations

First and last equations: Let

$$M_{i,\text{out}} = \sum_{j \wedge i} M_{i \to j} \quad \text{if } M_{i \to j} > 0,$$

then **for all tracer particles** in cell i:

$$p_{i,\text{out}} = \frac{M_{i,\text{out}}}{M_i}, \quad \# \text{ Proba. of going out of } i \tag{2}$$

$$p_{i \to j} = \frac{M_{i \to j}}{M_{i,\text{out}}}, \quad \# \text{ Proba. of going from } i \text{ to } j \tag{3}$$

following *S.Genel et al, 13*

Algorithm

Algorithm for cell i mass M_i, neighbors j:

1. Compute outgoing mass $M_{i,\text{out}}$ and $M_{i \to j}$.

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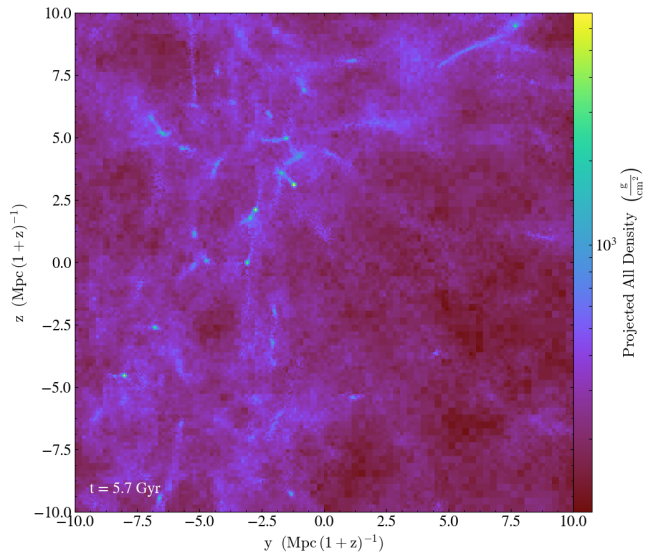
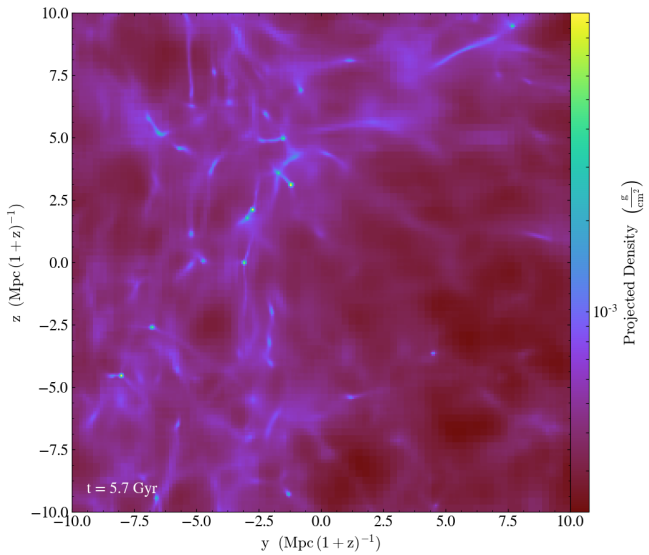
Small flux limit: $N_{\text{moved}} \sim$ Poisson distribution(p)

Is it working?

Cosmo


t = 5.7 Gyr
z (Mpc (1 + z)^−1)
y (Mpc (1 + z)^−1)
Projected All Density (g/cm^2)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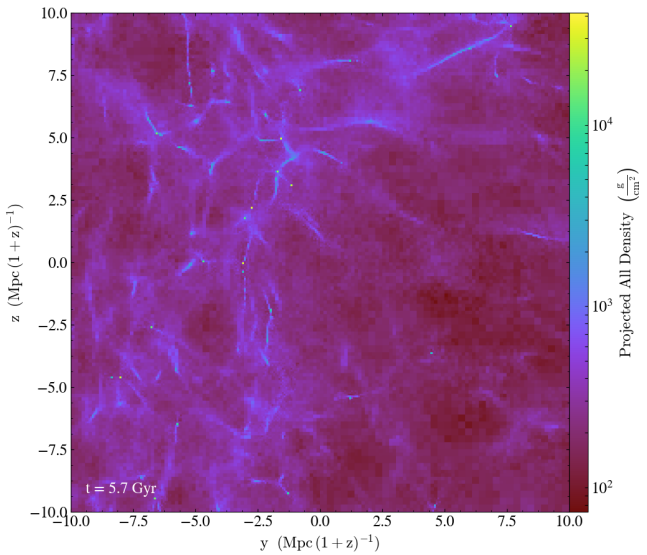
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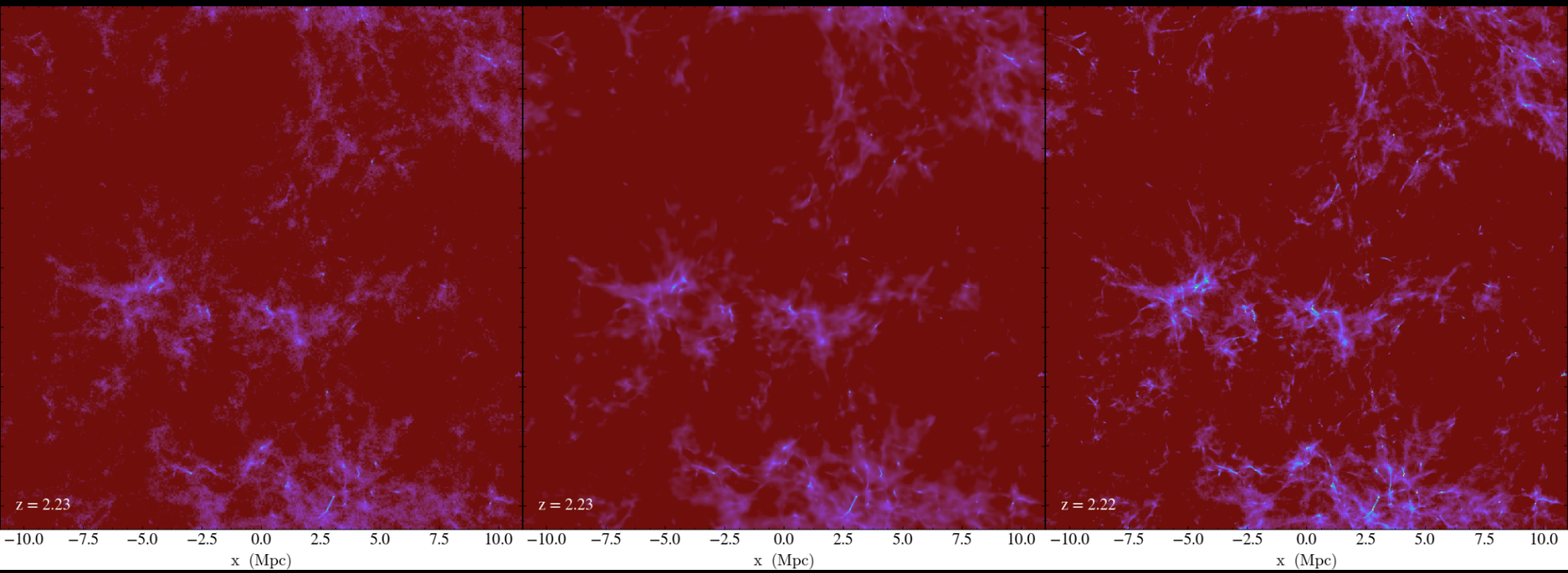
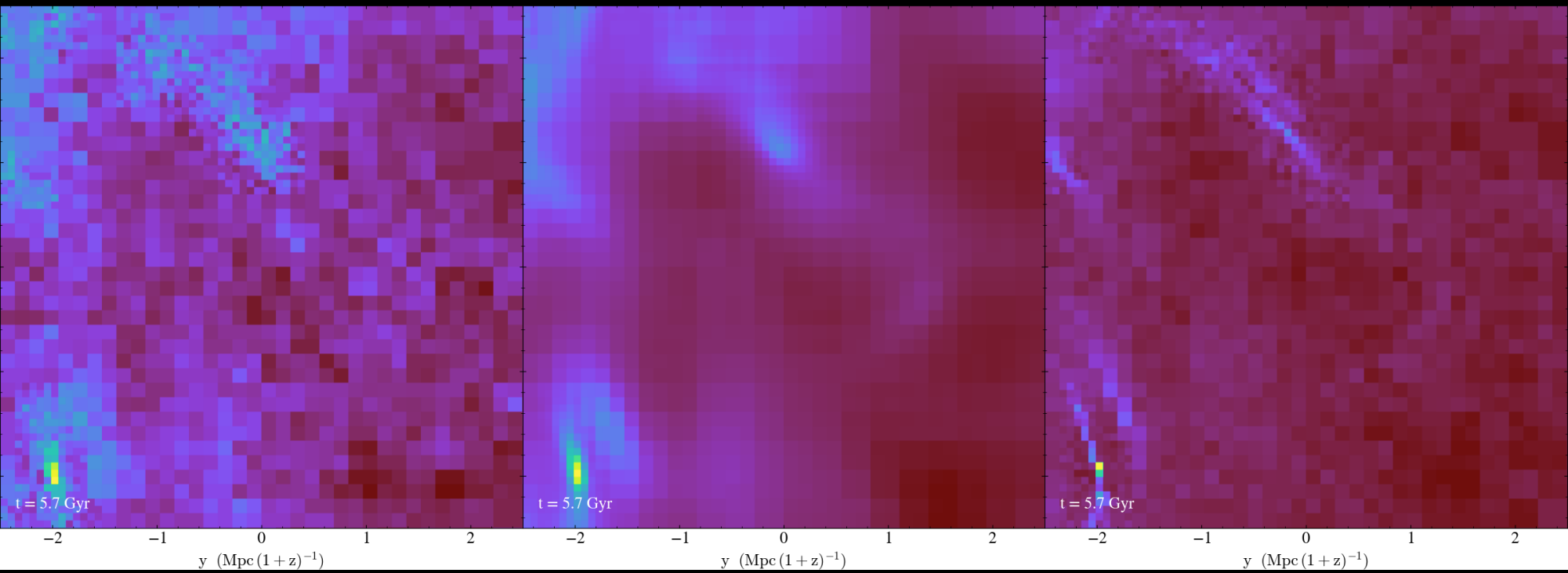


Cosmological Simulation, DM+hydro, left to right: MC tracer, gas and velocity tracers



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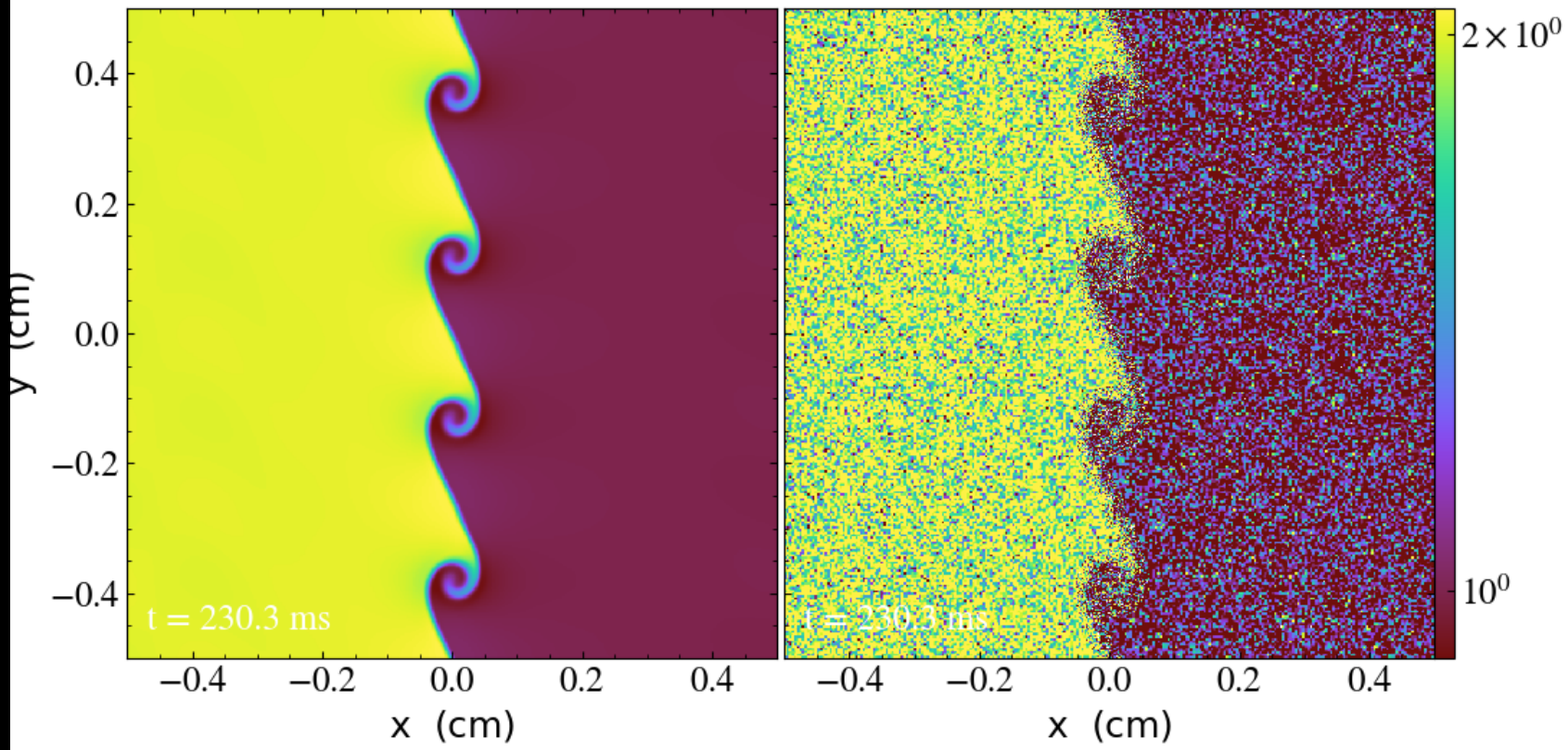
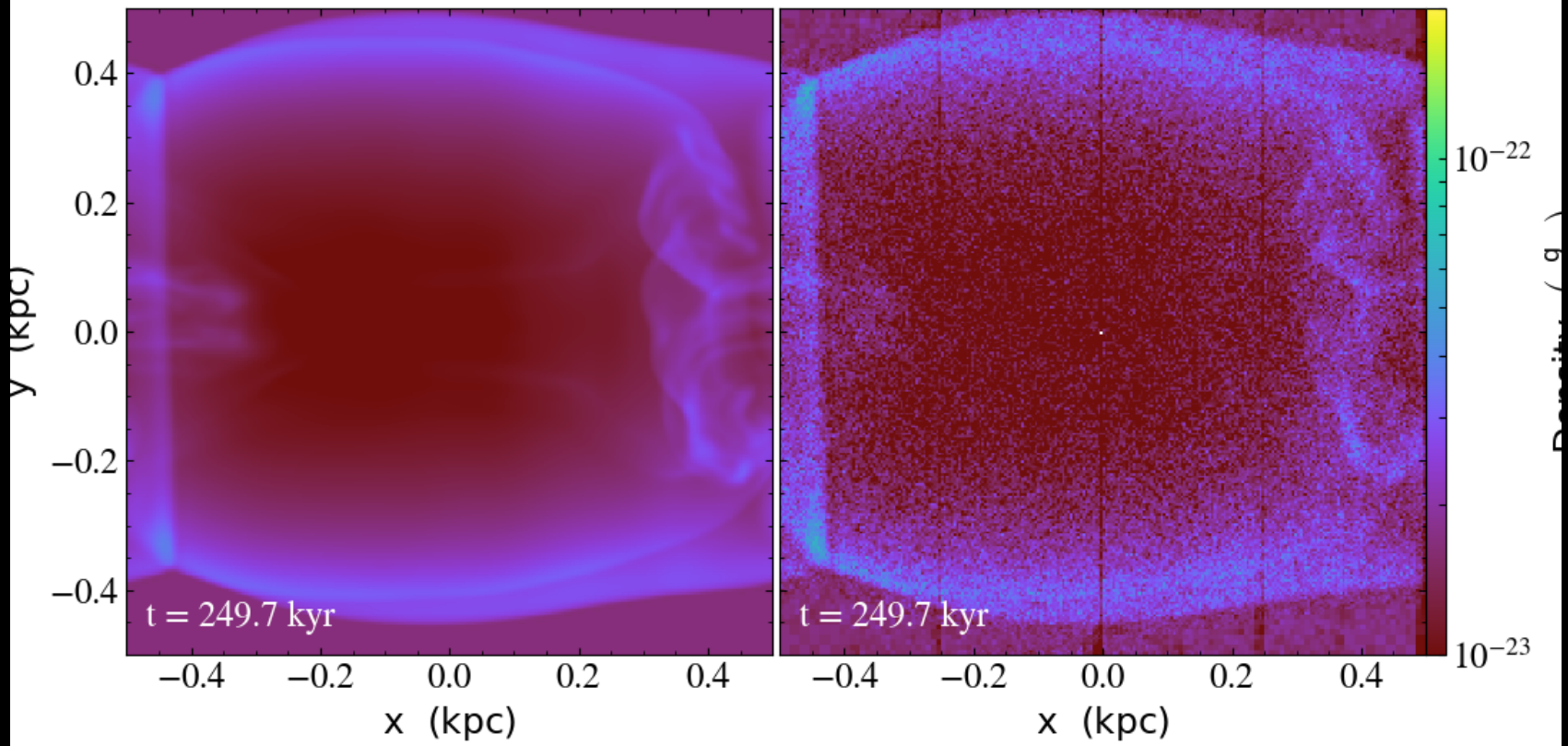
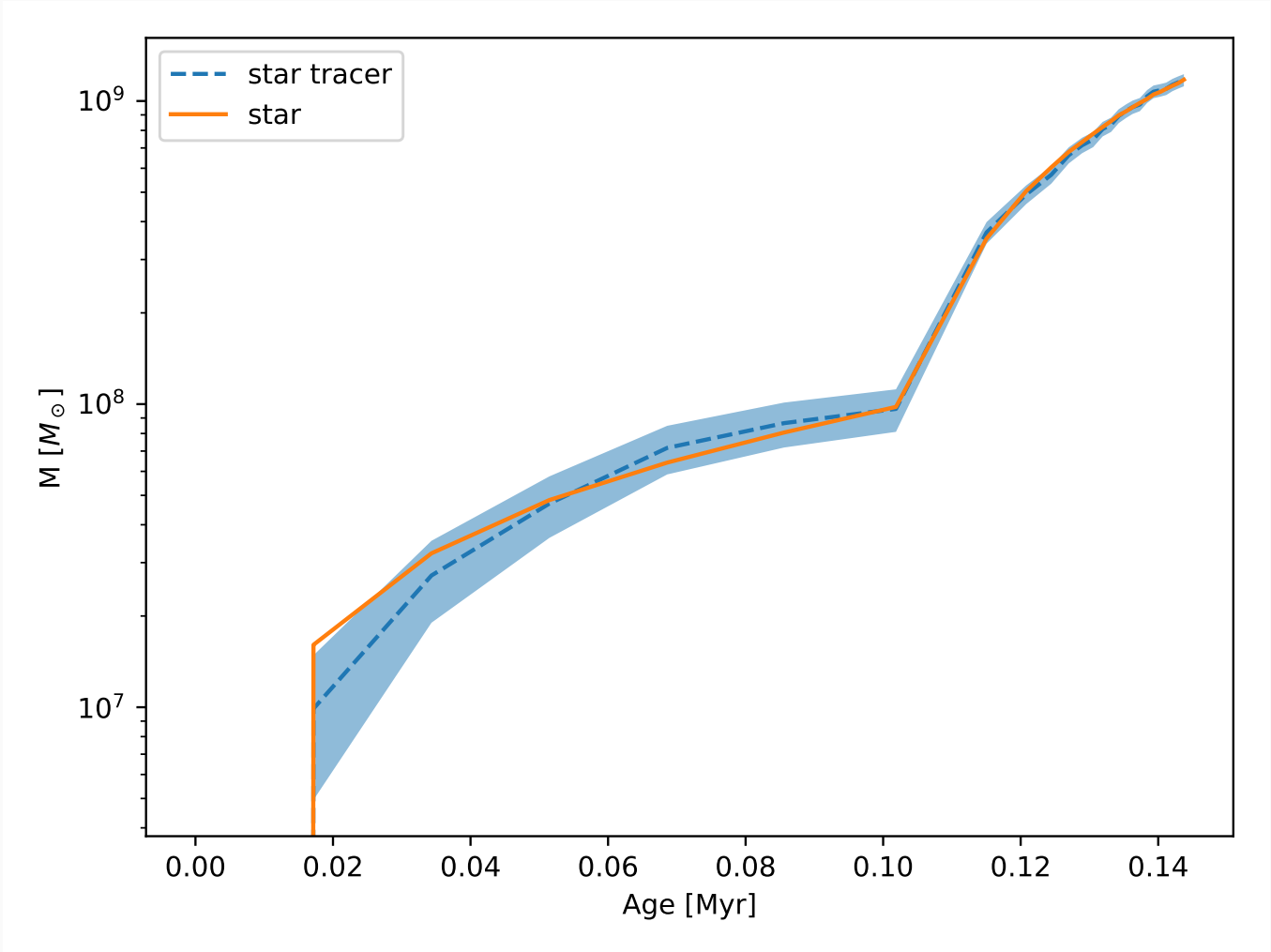

0.4
0.2
0.0
−0.2
−0.4
y (cm)
t = 230.3 ms
t = 230.3 ms
−0.4
−0.2
0.0
0.2
0.4
x (cm)
x (cm)
2×10^0
10^0


0.4
0.2
0.0
−0.2
−0.4
y (kpc)
t = 249.7 kyr
t = 249.7 kyr
−0.4
−0.2
0.0
0.2
0.4
x (kpc)
x (kpc)
10^{-22}
10^{-23}

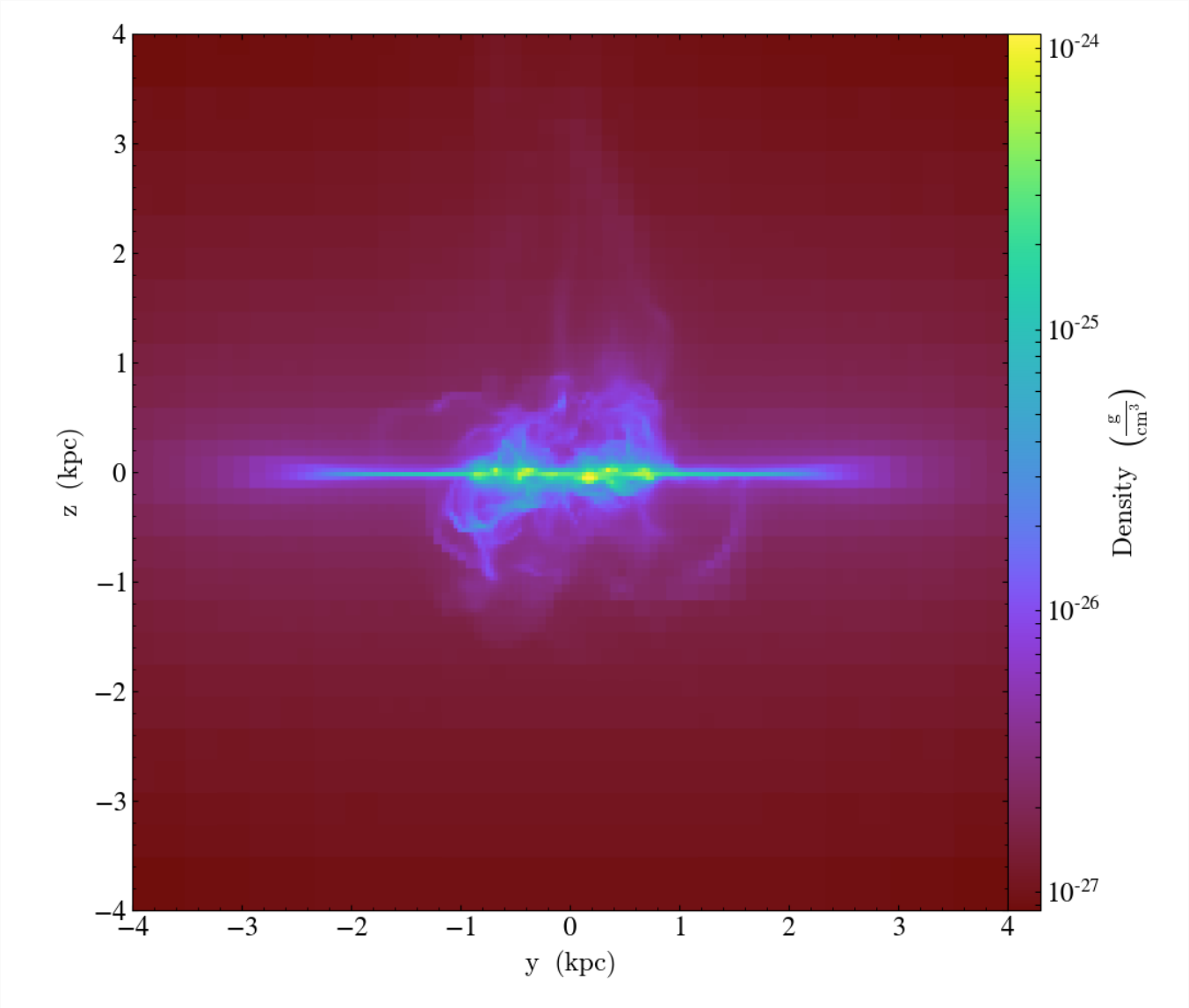
Star formation

- SF recipy: mechanical feedback
- homogeneous density



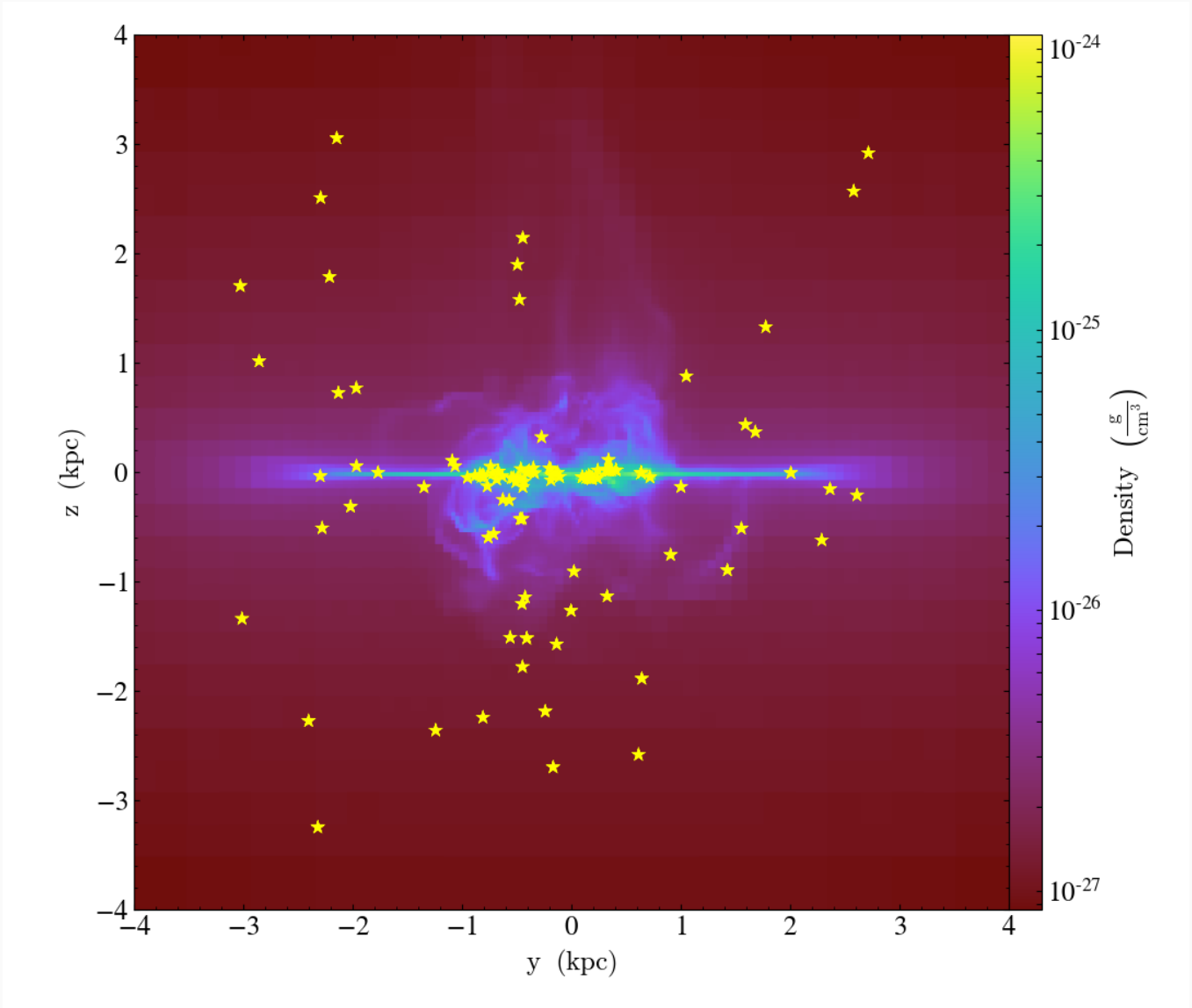
Small galaxy

Gas only



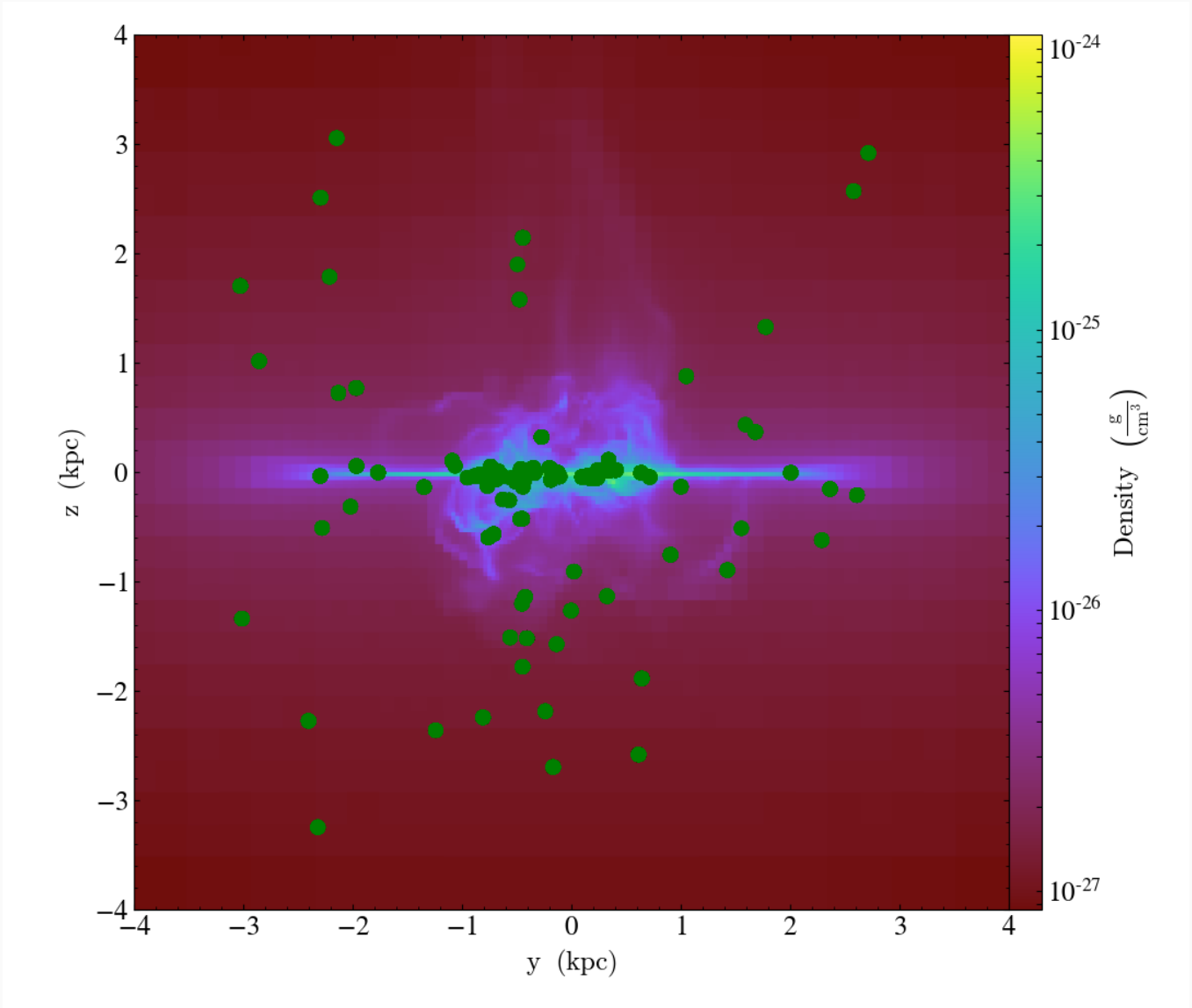
Small galaxy

Gas and stars



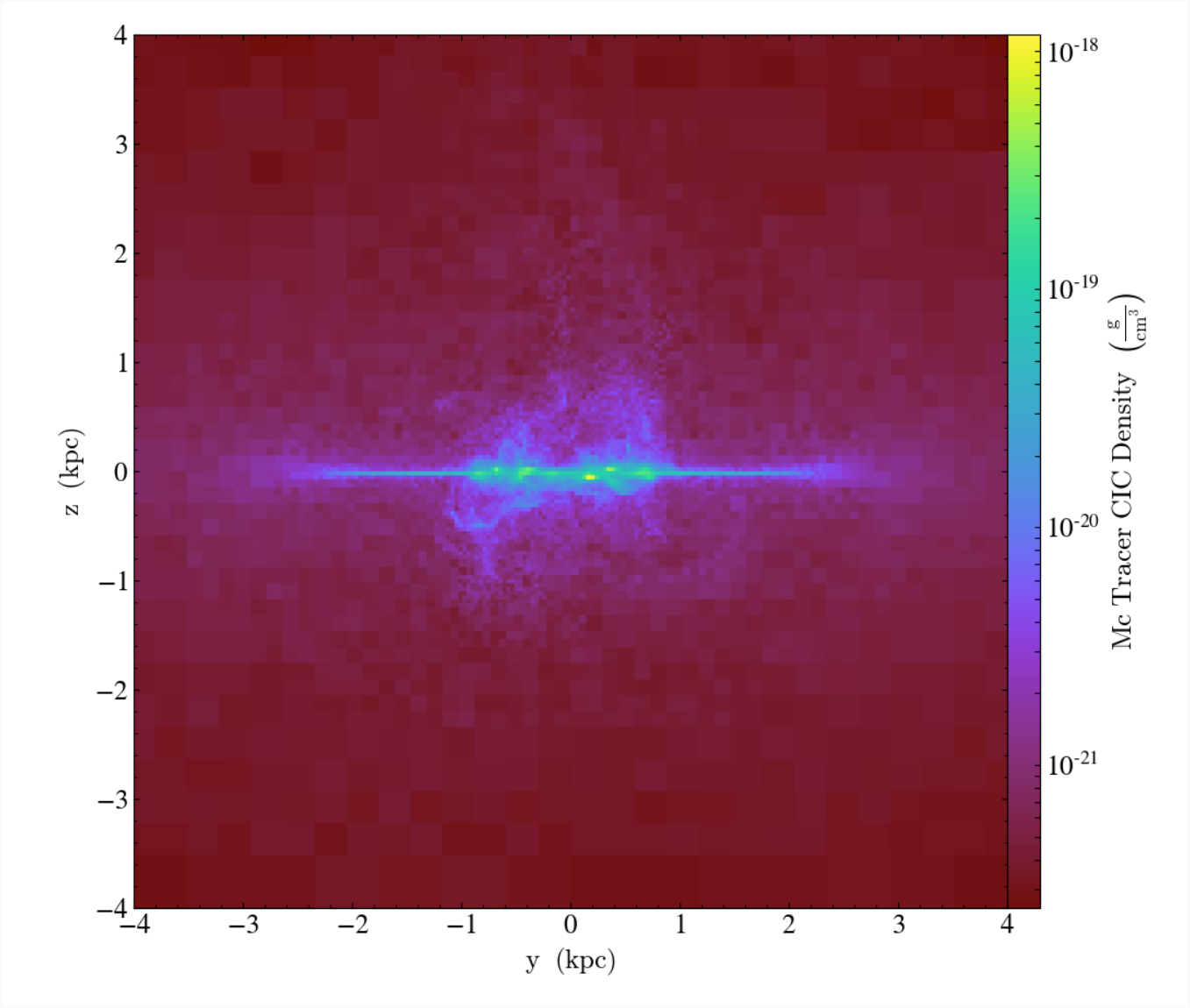
Small galaxy

Gas and star tracers



Small galaxy

MC tracers



Discussion

Room for improvement

TODO & wishlist:

- Get AGN feedback done (WIP).
- Other SN feedback.
- Quantify diffusion (esp. high flux limit)
- Explore other MC algorithms.

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- Get AGN feedback done (WIP).
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- Explore other MC algorithms.
- Get users!

"SAV" at corentin.cadiou@iap.fr

Thank you!

Questions?

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YT!

yt now supports:

- sinks
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- custom particle + fluid fields
- BSD license (permissive)

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